

Seismic fragility assessment of SMA-bar restrained multi-span continuous highway bridge isolated by high damping rubber bearings in medium to strong seismic risk zones

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ABSTRACT: An analytical method for conducting seismic fragility assessment of a three-span continuous highway bridge fitted shape memory alloy restrainers and isolated by laminated rubber bearings is discussed. Fragility functions, which express the likelihood of exceeding a damage state conditioned at a given earthquake intensity, are derived based on nonlinear incremental dynamic time history analyses results of the bridge subjected to medium to strong earthquake excitation records. A total of 20 excitation records with PGA values ranging from 0.45g to 1.07g, are used in the analysis. A 2-D finite element model scheme with nonlinearity force displacement relations for the bridge piers and the isolation bearings is used. The fragility curves are constructed for two bridge components: piers and isolation bearings. The numerical results show that the failure probability of the bridge is dominated by the bridge piers over the isolation bearings. Moreover, it is observed that the inclusion of SMA restrainers into the bridge system augments high probability of failure of the bridge piers and isolation bearings.

1 INTRODUCTION

Highway bridges are the most common and critical civil infrastructure components of a transportation network as they play important roles in evacuation and emergency routes for rescues, first-aid, firefighting, medical services and transporting disaster commodities. However, they are very vulnerable to damage during major earthquakes (Basoz and Kiremidjian, 1999; Yamazaki et al., 2000). Past and recent earthquakes, such as the 1971 San Fernando earthquake, the 1994 Northridge earthquake, the 1995 Great Hanshin earthquake in Japan, and the 1999 Chi-Chi earthquake in Taiwan, the 2008 Sichuan earthquake, the 2010 Chile earthquake, the 2010 Haiti earthquake, the 2011 Christchurch earthquake 2010 have shown the devastating nature of large earthquakes and its related economic impact.

In order to improve the seismic performance and subsequently reduce the seismic vulnerability of both new and retrofitted bridges, different forms of seismic isolation devices have been widely used for the last few decades (Buckle and Mayes, 1990; Naeim and Kelly, 1996; Skinner et al., 1993). Due to the flexible property of such isolation devices, the natural period of a bridge fitted with such a device can be increased in such way that the bridge resonance can be safely avoided. In addition, the inherently occupied damping property and energy dissipation mechanism prevents the bridge system from over displacement (Kelly, 1997). Field evidence on the seismic response of isolated bridges during recent earthquakes (Chaudaury et al., 2001), analytical studies (Diceli and Buddaram, 2006; Karim and Yamazaki, 2007; Ozbulut and Hurlebaus, 2011; Wilde et al., 2000; Zhang and Huo, 2009; Zhang et al., 2009) and experimental research (Kikuchi and Aiken, 1997; Hwang et al., 2002) have shown that isolation devices can suppress the transmission of the input earthquake energy, which helps improve the seismic performance and subsequently reduce the cost for repair and rehabilitation after earthquakes.

Laminated rubber bearings and sliding bearings are the two major types of seismic isolation devices, which are usually adopted for highway bridges. Due to the capability of supporting large loads while sustaining large movements with little or no maintenance requirement (Ali and Ghaffar, 1995), the laminated rubber bearings have been applied more frequently in highway bridges in recent years. Three types of laminated rubber bearings are widely used for this purpose: natural rubber bearing (NRB), lead rubber bearing (LRB), and high damping rubber bearing (HDRB). Out of these, HDRB, due to their high damping properties, are being

widely used all over the world, especially in Japan and USA. High damping rubber bearings possess various mechanical properties, which are influenced by their compounding effect (Hwang et al., 2002), nonlinear elasto-plastic behavior (Abe et al., 2004; Bhuiyan, 2009) and temperature and strain-rate dependent viscosity property (Bhuiyan, 2009; Bhuiyan et al., 2009; Dall’Asta and Ragni, 2006). Consequently, HDRB initiate some inherited problems, such as (i) instability due to large deformation, and (ii) un-recovered residual deformation, and (iii) the necessity for replacement of the deformed bearings after a strong earthquake. In order to overcome fully/partially the above mentioned limitations of the high damping rubber bearings, shape memory alloys (SMA) accompanied with laminated rubber bearings are reported to employ in the seismic isolation of highway bridge (DesRoches and Delemont, 2002; Ozbulut and Hurlebaus, 2011; Wilde et al., 2000). The super-elasticity and hysteresis property of the SMA allows it to incorporate with laminated rubber bearings to reduce the residual deformation of the bridge system.

The objective of this work is to carry out the seismic vulnerability assessment of a three-span continuous highway bridge isolated by high damping rubber bearings and SMA restrainers. In this regard, analytical simulation method is used to evaluate the seismic fragility of the bridge based on the results as obtained by nonlinear incremental dynamic analysis (IDA). A 2-D finite element model scheme with nonlinear force-displacement relationships for the bridge piers and the isolation bearings are used in analytical modeling of the bridge. Nonlinear incremental dynamic analyses of the isolated bridge are then performed for a total of 20 earthquake excitations of peak ground accelerations (PGA) magnitudes ranging from 0.45g to 1.07g. Each record is first scaled at selective earthquake intensities up to 2.0 g and then incremental dynamic analysis is carried out at each level of intensity. The seismic responses of the bridge components (pier and isolation bearing) are utilized to evaluate the likelihood of exceeding the seismic capacity of each component.

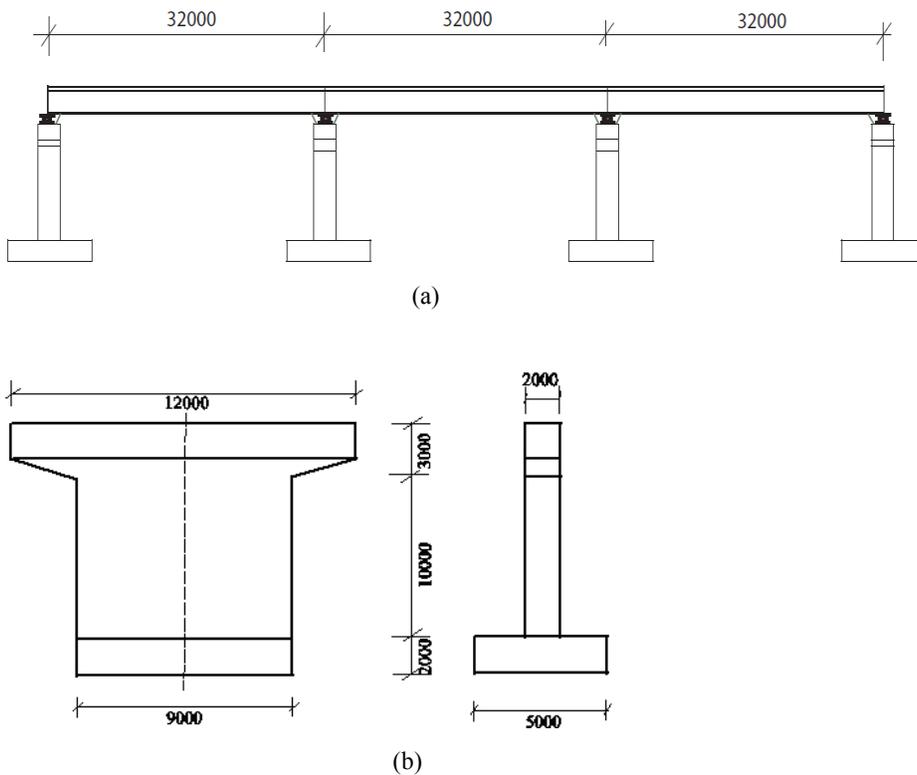


Figure 1. Geometric details of the bridge (a) longitudinal view of the bridge, and (b) transverse and longitudinal view of the bridge pier; all dimensions are in mm.

2 MODELING OF BRIDGE

2.1 Physical Model

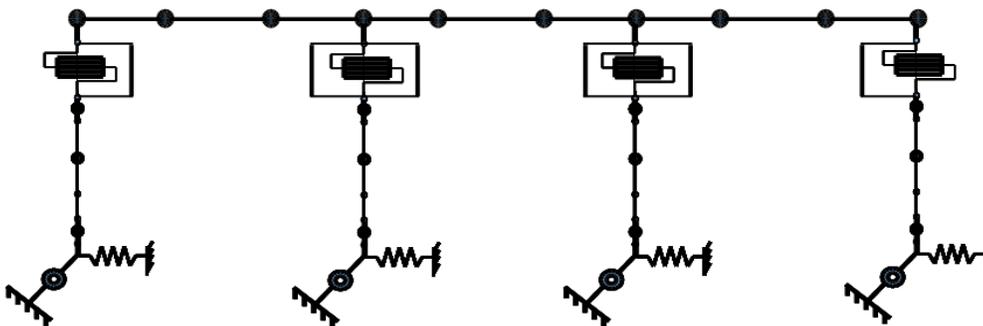
A typical three-span continuous highway bridge, isolated by laminated rubber bearings and SMA restrainers, is used in the current study as shown in Figures 1 (a) and (b). As can be presented in Figure 1, the bridge consists of continuous reinforced concrete (RC) deck-steel girder isolated by laminated rubber bearings installed below the steel girder supported on RC piers. In addition, two SMA bars are used at each bridge

pier being attached between the top of bridge pier and bottom of the girder. The superstructure consists of 260 mm RC slab covered by 80 mm of asphalt layer.

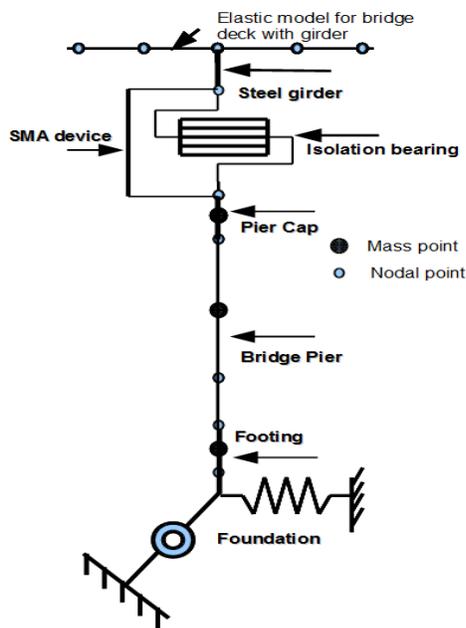
The height of the continuous steel girder is 1800 mm. The substructures consist of RC piers and footings supported on shallow foundation. The reinforcement details of the bridge pier consist of D29 (diameter 29 mm) longitudinal reinforcements along the longer direction being distributed @ 200 mm c/c except at the corners where the spacing of the reinforcements is 125 mm c/c and D29 (diameter 29 mm) reinforcements along the shorter direction being distributed @ 200 mm c/c except at the corners where spacing is limited to 150 mm c/c. The hoop reinforcements in both directions are D22 (diameter 22 mm) being distributed @ 125 mm c/c. The dimensions and material properties of the bridge deck, piers with footings are given in Table 1. The geometry and material properties of laminated rubber bearings and shape memory alloy are presented in Table 2.

Table 1. Geometries and material properties of the bridge

Properties	Specifications
Cross-section area of the pier cap (mm^2)	2000x12000
Cross-section area of the pier body (mm^2)	2000x9000
Cross-section area of the footing (mm^2)	5000x9000
Height of the pier (mm)	15000
Young's modulus of elasticity of concrete (N/mm^2)	25000
Young's modulus of elasticity of steel (N/mm^2)	200000



(a)



(b)

Figure 2. Analytical model of the bridge system (a) 2-D finite element model of the bridge system including nonlinear model used for isolation bearings and bridge pier, and (b) details of modeling of an internal bridge pier.

Table 2. Geometries and materials properties of the isolation bearings and Ni-Ti SMA

Dimension	Specifications	
	HDRB	LRB
Cross-section of the bearing (mm ²)	600	600
Thickness of rubber layers (mm)	81	75
Number of rubber layers	6	6
Thickness of steel layer (mm)	3.0	3.0
Nominal shear Modulus (MPa)	1.2	1.2
Number of lead plugs	-	4
Diameter of lead plugs (mm)	-	90
Cross-section of SMA restrainer bar (mm ²)		1256
Length of SMA restrainer bar (mm)		2500

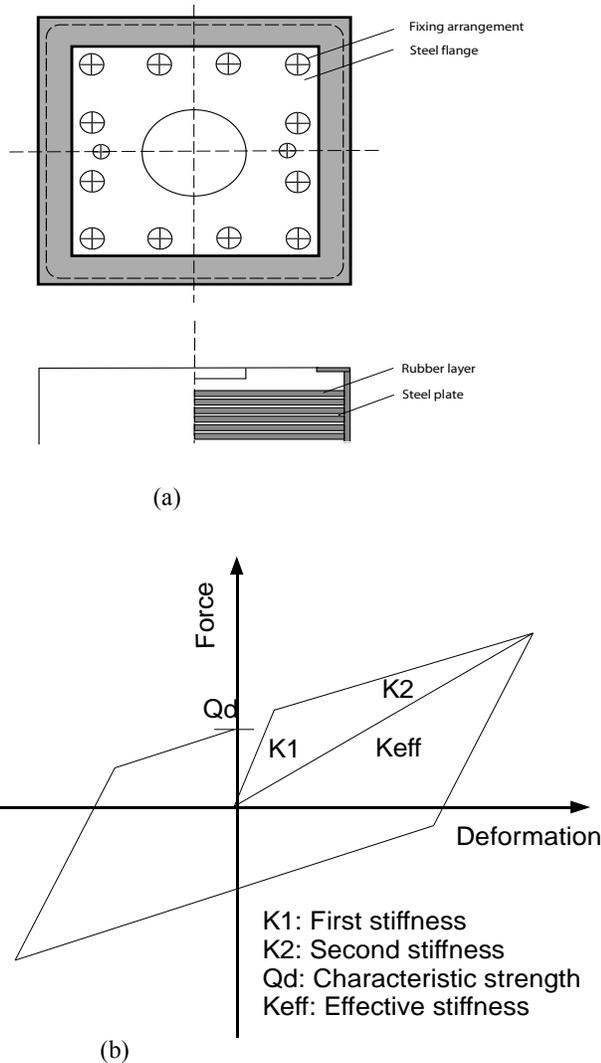


Figure 3. (a) Typical arrangement of HDRB, (b) typical arrangement of LRB, and (c) bilinear model of laminated rubber bearing as used in AASHTO (2000) and JRA (2002).

2.2 Analytical Model

The analytical model of the bridge system is shown in Figure 2(a). The entire system is approximated as a continuous 2-D finite element frame using the SeismoStruct nonlinear analysis program (SeismoStruct, 2011). A finite element model with frame and spring elements is used to approximate the continuous system with a finite number of degrees of freedom. The superstructure and substructure of the bridge are modeled as a lumped mass system divided into a number of small discrete segments. The mass of each segment is as-

sumed to be distributed between the two adjacent nodes in the form of point mass. The details of modeling of a typical bridge pier along with deck are given in Figure 2 (b).

The superstructure consisting of RC bridge deck and steel girders is modeled using linear beam-column elements so that the superstructure remains elastic under the seismic loads applied in the longitudinal direction. It should be noted that the stiffness of the superstructure does not have a significant effect on the seismic response of the bridge (Ghobarah and Ali, 1988) since the longitudinal response is typically governed by the isolation bearings, bridge piers, and foundation (Choi et al., 2004). The bridge piers are modeled using the fiber elements. Each fiber has a stress–strain relationship, which can be specified to represent unconfined concrete, confined concrete, and longitudinal steel reinforcement. The confinement effect of the concrete section is considered on the basis of reinforcement detailing as discussed in the preceding section. The distribution of inelastic deformation and forces is sampled by specifying cross-section slices along the length of the element. The pier footings are modeled using linear elastic elements. The footing–foundation movement is modeled using two linear translation and rotation springs.

High damping rubber bearings (HDRB) and lead rubber bearings (LRB). The mechanical behavior of laminated rubber bearings, especially HDRBs, are mainly dominated by strain magnitude (Abe et al., 2004, Bhuiyan et al., 2009), strain-rate (Bhuiyan et al., 2009, Dall’Asta and Ragni, 2006) and also compounding effect (Hwang et al. 2002) etc. Moreover, the mechanical behavior of laminated rubber bearings can be characterized by three distinct features: a high initial stiffness at very small strain levels, an almost constant stiffness at small to medium strain levels followed by a high stiffness due to its inherently occupied strain hardening features. So, a constitutive model to be capable of replicating the strain-rate and the strain level dependent mechanical behavior of laminated rubber bearing is required for simulating the mechanical responses when subjected to earthquake induced ground motions. However, for brevity, the current study considers the design bilinear model (Figure 3) as proposed in code specifications (AASHTO, 2000; JRA, 2002). The model parameters of the bearings are estimated as per recommendations of JRA (2002) and presented in Table 3.

In general, the constitutive model of SMA is very complicated in a sense that it depends upon many factors, such as strain rates (Auricchio et al., 1997), strain magnitude and strain history (Wei et al., 2002). Three categories of constitutive models are used for characterizing the superelasticity and damping properties of SMA, such as parametric, nonparametric and differential equation-based models. However, the differential equation-based constitutive model (Auricchio et al., 1997; Wei et al., 2002) is widely used for SMA since it is capable of using in continuum mechanics based FE algorithms considering small and finite deformations and subsequently in finite element based professional software packages, such as ANSYS (2010) and SeismoStruct (2011), etc. Table 4 shows the parameters of Ni-Ti based SMA (Figure 4) used in the analysis of this study.

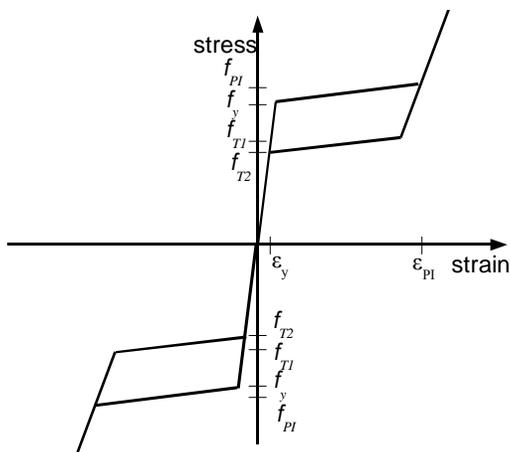


Figure 4. A typical one-dimensional superelastic model of shape memory alloy with its characteristic stress and strain.

Table 3. Design parameters of HDRB

	HDRB	LRB
Elastic stiffness, K1 (kN/m)	36000	30000
Post yield stiffness, K2, (kN/m)	4173	4221
Characteristic strength, Qd (kN)	212	200
Effective stiffness, Keff (kN/m)	5791	5840
Effective damping ratio (%)	16.9	16.7

Table 4. Constitutive parameters of Ni-Ti based SMA

Parameters	Unit	Value
Austenite to martensite starting stress, f_v	MPa	410
Austenite to martensite finishing stress, f_{P1}	MPa	470
Martensite to austenite starting stress, f_{T1}	MPa	170
Martensite to austenite finishing stress, f_{T2}	MPa	140
Yield strain limit, ε_v	%	1
Recoverable pseudoelastic strain limit, ε_{PI}	%	7

3 SEISMIC FRAGILITY FUNCTION

Many analytical methods have been utilized to derive analytical fragility functions for expressing seismic vulnerability of the bridge, which include elastic spectral analyses nonlinear static analyses, and linear/nonlinear time-history analyses. This study employs Probabilistic Seismic Demand Model (PSDM) to derive the analytical fragility curves using nonlinear time-history analyses of the bridge system. The PSDM establishes a correlation between the engineering demand parameters (EDP) and the ground intensity measures (IM). In the current study, the ductility of bridge pier and horizontal deformation of isolation bearing are considered as the two EDPs, and the peak ground acceleration (PGA) is utilized as intensity measure (IM) of each ground motion record. Two approaches are used to develop the PSDM: the scaling approach (Zhang and Huo, 2009) and the cloud approach (Choi et al., 2004). In the scaling approach, all the ground motions are scaled to selective intensity levels and an incremental dynamic analysis (IDA) is conducted at each level of intensity; however, in the cloud approach, un-scaled earthquake ground motions are used in the nonlinear time-history analysis and then a probabilistic seismic demand model is developed based on the nonlinear time history analyses results. In the current study, only the IDA method is utilized in evaluating the seismic fragility functions of the bridge components and system as well. The IDA method requires more computational efforts in scaling of earthquake ground motion records to be applied in nonlinear time history analysis at each IM level. In this approach, no priori assumption needs to be made in terms of probabilistic distribution of seismic demand in order to derive the fragility curves. In the current study, every ground motion record is scaled up to a maximum PGA of 2.0g to be applied in IDA method. The occurrence ratio at a specified damage state (DS) is computed and directly used as the damage probability at the given IM level, i.e. the damage probability is calculated as the ratio of the number of damage cases n_i for the damage state i over the number of total simulation cases N :

$$P[EDP > DS_i | IM] = \frac{n_i}{N} \quad (1)$$

The fragility curves as derived using IDA approach can be expressed in most cases using a lognormal cumulative distribution function:

$$P[EDP > DS_i | IM] = \int_{-\infty}^{IM} \frac{1}{IM \sqrt{2\pi\xi_{IM}^2}} \exp\left[-\frac{[\ln(IM) - \lambda]^2}{2\xi_{IM}^2}\right] d(IM), \quad (2)$$

where λ and ξ^2 denotes mean and standard deviation of IMs based of lognormal distribution.

4 CHARACTERIZATIONS OF DAMAGE STATES

For seismically isolated highway bridges with continuous composite deck-girder system, bridge piers and isolation bearings are the most critical components, which are often forced to enter into nonlinear range of deformations under strong earthquakes. Different forms of EDPs, ductility for bridge piers and horizontal deformation for isolation bearings, are used to measure the damage state (DS) of the bridge components. A capacity model is needed to measure the damage of bridge component based on prescriptive and descriptive damage states in terms of EDPs (FEMA, 2003, Choi et al., 2004, Nielson, 2005). Four damage states as defined by HAZUS (FEMA, 2003) are commonly adopted in the seismic vulnerability assessment of engineering structures, namely slight, moderate, extended and collapse damages. Table 5 summarizes the definitions of various damage states and their corresponding damage criteria available in literature. The damage states of isolation devices are determined based on experimental observation as well as the consideration of resulting pounding and unseating. Typically either the bearing displacement or shear strain is used to describe the damage states, as shown in Table 5.

Previous studies (Abe et al., 2004, Bhuiyan, 2009) show that the mechanical behavior of laminated rubber bearings portrays three distinct features such as initial high stiffness at very low strain levels, almost constant stiffness at low to moderate strain levels due its Payne's effect and finally high stiffness at high strain levels (e.g. 150%) due to its strain hardening effects. Moreover, strain-rate and temperature induced viscosity property is depicted in the bearings, especially in high damping rubber bearings (Bhuiyan et al., 2009, Bhuiyan, 2009). Although the modern isolation bearings can experience shear strain up to 400% before failure, such large shear strain will result in large displacement and can cause significant pounding or unseating problem in the bridge system. Therefore, once the shear strain exceeds 250%, it is considered as complete damage of the bearing (JRA, 2002). In this study, the shear strain for isolation bearings and the displacement ductility for the bridge pier are adopted as damage index (DI) to capture the damage states.

5 SEISMIC GROUND MOTION RECORDS

A suite of 20 earthquake ground motion records (Figure 5), which are assigned as medium to strong magnitude earthquake ground motions (JRA, 2002), with PGA values ranging from 0.45g to 1.07g have been considered in the current study. Figure 6 shows the acceleration response spectra with 5 percent damping ratio of the recorded ground motions. The mean amplitude of the earthquake records is shown by solid thick line in the figure.

Table 5. Damage/limit state of bridge components

Damage State →		Slight (DS=1)	Moderate (DS=2)	Extensive (DS=3)	Collapse (DS=4)	Reference
Bridge components	Physical phenomenon	Cracking and spalling	Moderate cracking and spalling	Degradation without collapse	Failure leading to collapse	FEMA, 2003
Bridge pier	Section ductility μ_k	$\mu_k > 1$	$\mu_k > 2$	$\mu_k > 4$	$\mu_k > 7$	Choi et al. 2004
	Displacement ductility μ_d	$\mu_d > 1.0$	$\mu_d > 1.2$	$\mu_d > 1.76$	$\mu_d > 4.7$	Hwang et al. 2001
	Displacement δ (mm)	$\delta > 0$	$\delta > 50$	$\delta > 100$	$\delta > 150$	Choi et al. 2004
Isolation bearing	Shear strain γ (%)	$\gamma > 10$	$\gamma > 15$	$\gamma > 200$	$\gamma > 250$	Zhang and Huo 2009

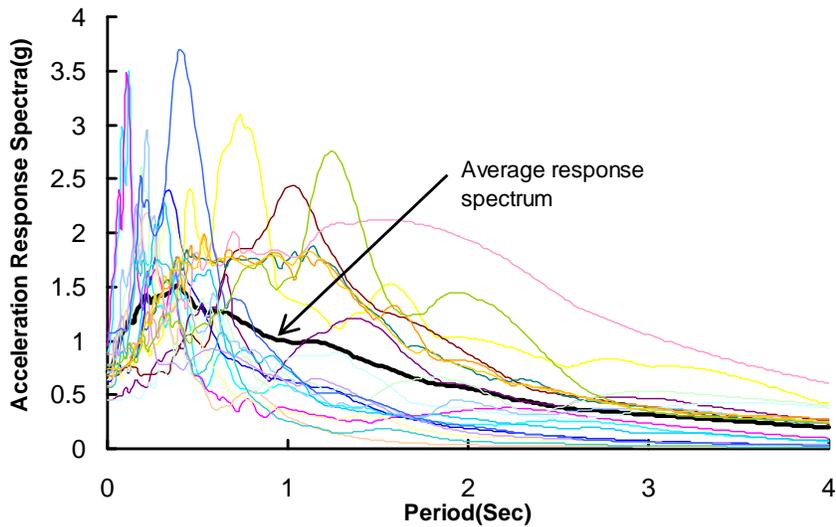
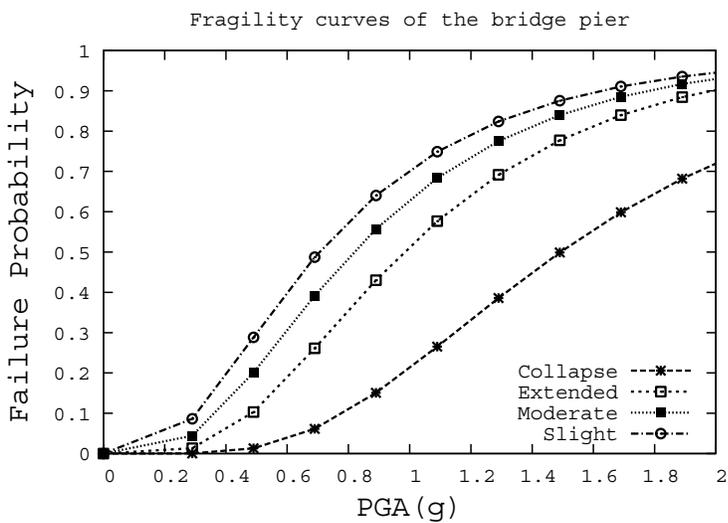
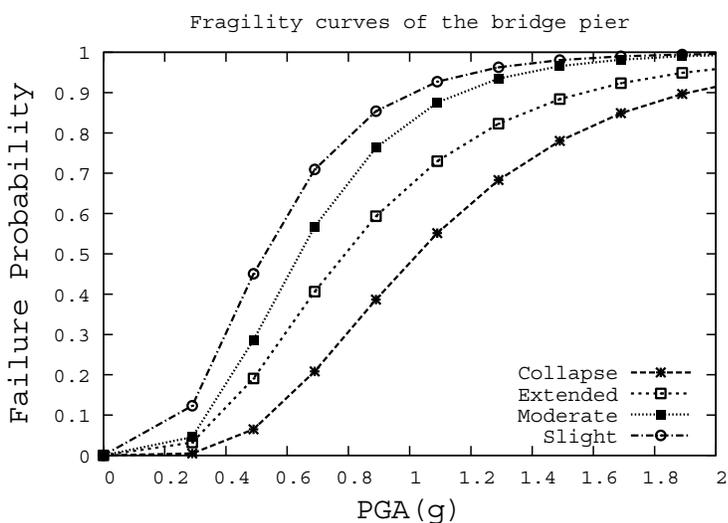


Figure 5. Response acceleration spectra of a suit of 20 near filed earthquake ground motion records. The values peak ground accelerations range from 0.45g to 1.07g.



(a)



(b)

Figure 6. Fragility curves of the bridge pier isolated with high damping rubber bearings (a) without SMA restrainers and (b) with SMA restrainers

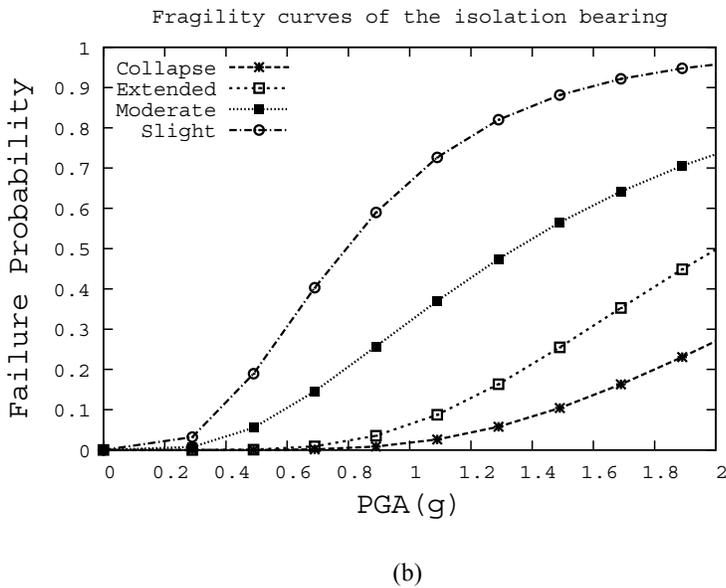
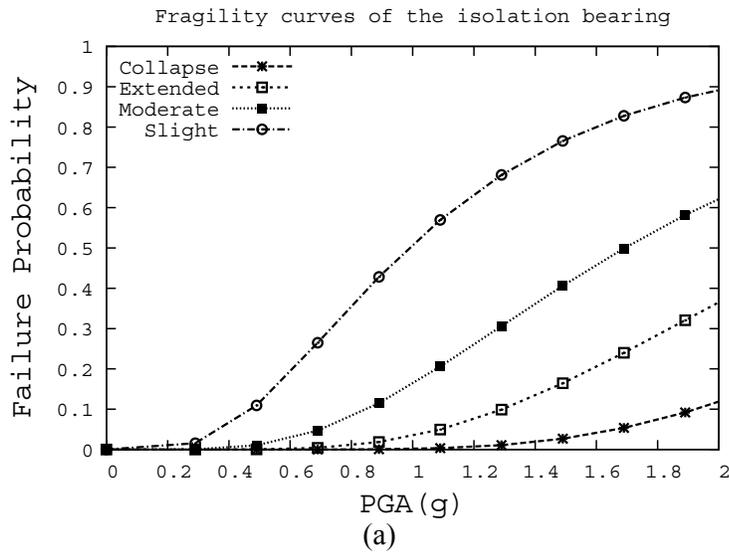


Figure 7. Fragility curves of the isolation system using high damping rubber bearings (a) without SMA restrainers (b) with restrainers.

6 NUMERICAL RESULTS AND DISCUSSION

In order to assess the seismic vulnerability of a three-span continuous highway bridge, seismic fragility curves for the piers and isolation bearings are generated using the numerical results obtained from the nonlinear incremental dynamic analysis. The bridge is isolated with two types of laminated rubber bearings along with shape memory alloy restrainers. Assuming a lognormal distribution with respect to the median of seismic intensity (PGA), the fragility curves for two bridge components, pier and isolation bearing, are generated using Eqs.(1) and (2) and calibrating with the capacity limit states as shown in Table 1. In this regard, a number of incremental dynamic analyses of the bridge, subjected to longitudinal excitations using 20 ground motion records of PGA magnitudes ranging from 0.45 to 1.07g, are carried out. Each ground motion record is scaled at different intensity levels up to 2.0g PGA, which is then used in the incremental dynamic analysis. Nonlinear model for bridge piers and isolation bearings as well shape memory alloys is considered in the analysis. Moreover, the Raleigh damping approach is employed in order to estimate the damping of the bridge.

Figures 6 and 7 present the fragility curves of the bridge at component levels, i.e. bridge piers and isolation bearings. Figures 6 (a) and (b) present the fragility curves for the bridge pier isolated by HDRB without and with SMA restrainers, respectively. The most vulnerable pier is considered in deriving the fragility curves

for different damage states (DS) as recommended by HAZUS-MH (FEMA, 2003), such as *slight, medium, extended and collapse*. As can be observed from Figs. 6(a) and (b), the inclusion of SMA device in the isolation system significantly increases the seismic vulnerability of the bridge pier in all damage states at each earthquake intensity level. This can be attributed that the inclusion of SMA device induces an additional stiffness to the bridge system causing a higher seismic force demand being attracted to the bridge pier [Wilde *et al.*, 2000].

Figures 7 (a) and (b) display the fragility curves for the HDRB without and with SMA restrainers. A total of four isolation bearings are used in the bridge to accommodate the vertical and lateral deformations as experienced from the vertical compressive loadings of the bridge deck and the earthquake ground motions. Only the most vulnerable bearing is utilized to derive the fragility curves. From each figure it is revealed that the inclusion of SMA restrainer in the isolation system causes a little increase in the seismic fragility of the HDRB for the given damage states, which further induces the seismic vulnerability of the bearing and the bridge deck.

7 CONCLUDING REMARKS

This study utilizes analytical simulation method to conduct seismic fragility assessment of a three-span continuous highway bridge fitted with SMA restrainer and base isolation bearings. The fragility curves for bridge components (pier and isolation bearing) are generated based on the IDA-based scaling approach using 20 near-field earthquake ground motion records. The numerical results generally show that bridge piers are more susceptible to the given seismic ground motions as compared to the isolation bearings. Specifically, the seismic fragility of the bridge pier and the system increases with the inclusion of the SMA restrainers in the isolation system. It is believed that the fragility curves as obtained for the bridge considered in the study can be used to estimate the potential losses incurred from earthquakes, retrofitting prioritization and post-earthquake rehabilitation decision making.

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